Practice Problems Unit 3

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Problem #1

In triangle ABC, angles A and B are 4:6 respectively, and the measure of angle C is 80 degrees. What is the measure of angle A?

Given angles A and B are 4:6, we can write that as m < A = 4x, and m < B = 6x. By triangle sum theorem, we know that m < A plus m < B plus m < C is equal to 180 degrees. Since m < C is 80 degrees, we can substitute it and our other values in to have $4x + 6x + 80^\circ = 180^\circ$, simplified as $10x + 80^\circ = 180^\circ$. Through the subtraction property of equality, we can subtract 80 from both sides, to get $10x = 100^\circ$. If we divide both sides by 10, we get $x = 10^\circ$. Congradulations! You aren't done! Remember, m < A is 4x, and 4 times 10 is 40, so the answer is. . . $m < A = 40^\circ$

Problem #2

Given AB is congruent to AC and m<A is 40°, what is the measure of the linear pair of <B?

Since AB is congruent to AC, we can tell that A is the vertex angle, and triangle ABC is isosceles. Since ABC is isosceles, the base angles (B and C) are congruent. Through triangle sum theorem, we can tell that <A plus <B plus <C is equal to 180°. By substitution, $40^\circ + <B + <C = 180^\circ$. If we subtract 40 from both sides, we get $<B + <C = 140^\circ$. Since <B and <C are of the same measure, we can say that they are 70° each. If m<B = 70°, the linear pair theorem means 180 - m<B is the measure of the linear pair. In other words, the measure of the linear pair of <B is 110°.